

Zuweisungsregel

$$\{P_E^x\} x := E \{P\}$$

Sequenzregel

$$\frac{\{P\} S_1 \{Q\}; \{Q\} S_2 \{R\}}{\{P\} S_1; S_2 \{R\}}$$

Iteration

$$\frac{\{P \wedge B\} S \{P\}}{\{P\} \text{ while } B \text{ do } S \{P \wedge \neg B\}}$$

$$\frac{\{P\} S \{Q\} \quad \{Q \wedge \neg B\} S \{Q\}}{\{P\} \text{ repeat } S \text{ until } B \{Q \wedge B\}}$$

Fallunterscheidung

$$\frac{\begin{array}{l} \{P \wedge B\} S \{Q\} \\ P \wedge \neg B \Rightarrow Q \end{array}}{\{P\} \text{ if } B \text{ then } S \{Q\}}$$

$$\begin{array}{l} \{P \wedge B\} S_1 \{Q\} \\ \{P \wedge \neg B\} S_2 \{Q\} \end{array}$$

$$\frac{\quad}{\{P\} \text{ if } B \text{ then } S_1 \text{ else } S_2 \{Q\}}$$

Implikation

$$\frac{\{P\} S \{Q\}, Q \Rightarrow R}{\{P\} S \{R\}}$$

$$\frac{P \Rightarrow R, \{R\} S \{Q\}}{\{P\} S \{Q\}}$$

$$P \equiv \{b \in \mathbb{Z} \wedge \forall i \in \mathbb{Z}, 0 \leq i < b < a.length : c \leq a[i] < d\}$$

if (a[b] <= c)

$$\{b \in \mathbb{Z} \wedge \forall i \in \mathbb{Z}, 0 \leq i < b < a.length : c \leq a[i] < d \wedge a[b] \leq c\}$$

$$\{b \in \mathbb{Z} \wedge \forall i \in \mathbb{Z}, 0 \leq i < b < a.length : a[b] \leq a[i] < d \wedge a[b] \leq c\}$$

c = a[b]

$$\{b \in \mathbb{Z} \wedge \forall i \in \mathbb{Z}, 0 \leq i < b < a.length : c \leq a[i] < d \wedge a[b] = c\}$$

$$\{b \in \mathbb{Z} \wedge \forall i \in \mathbb{Z}, 0 \leq i \leq b < a.length : c \leq a[i] < d\}$$

else

$$\{b \in \mathbb{Z} \wedge \forall i \in \mathbb{Z}, 0 \leq i < b < a.length : c \leq a[i] < d \wedge a[b] > c\}$$

d = a[b]

$$\{b \in \mathbb{Z} \wedge \forall i \in \mathbb{Z}, 0 \leq i \leq b < a.length : c \leq a[i] \wedge d > c\}$$

$$Q \equiv \{b \in \mathbb{Z} \wedge \forall i \in \mathbb{Z}, 0 \leq i \leq b < a.length : c \leq a[i]\}$$

$$\{a, b, c \in \mathbb{N}_0 \wedge a = 0 \wedge c = 1 \wedge c = 2^a\}$$

while (a < b)

$$\{a, b, c \in \mathbb{N}_0 \wedge c = 2^a \wedge a < b\}$$

$$\{a, b, c \in \mathbb{N}_0 \wedge 2c = 2^{a+1} \wedge a < b\}$$

c = 2 * c

$$\{a, b, c \in \mathbb{N}_0 \wedge c = 2^{a+1} \wedge a < b\}$$

a = a + 1

$$\{a, b, c \in \mathbb{N}_0 \wedge c = 2^a \wedge a \leq b\}$$

end while

$$\{a, b, c \in \mathbb{N}_0 \wedge c = 2^a \wedge a \leq b \wedge a \geq b\}$$

$$\{a, b, c \in \mathbb{N}_0 \wedge c = 2^a \wedge a = b\}$$

$$\frac{\{P \wedge B\} S \{P\}}{\{P\} \text{ while } B \text{ do } S \{P \wedge \neg B\}}$$

$P \equiv \{?\}$

if ($b > c$)

$P \wedge b > c$

$b = b/2$

$Q \equiv \{a = b\}$

else

$P \wedge b \leq c$

$a = a + 1$

$Q \equiv \{a = b\}$

$$\frac{\begin{array}{l} \{P \wedge B\} S_1 \{Q\} \\ \{P \wedge \neg B\} S_2 \{Q\} \end{array}}{\{P\} \text{ if } B \text{ then } S_1 \text{ else } S_2 \{Q\}}$$

$$P \equiv \{?\}$$

if (b>c)

$$a = b / 2 \wedge b > c$$

$$b = b / 2$$

$$Q \equiv \{a = b\}$$

else

$$a + 1 = b \wedge b \leq c$$

$$a = a + 1$$

$$Q \equiv \{a = b\}$$

$$\frac{\begin{array}{l} \{P \wedge B\} S_1 \{Q\} \\ \{P \wedge \neg B\} S_2 \{Q\} \end{array}}{\{P\} \text{if } B \text{ then } S_1 \text{ else } S_2 \{Q\}}$$

$$P \equiv \{a = b/2 \wedge b > c \vee a + 1 = b \wedge b \leq c\}$$

if ($b > c$)

$$a = b/2 \wedge b > c$$

$$b = b/2$$

$$Q \equiv \{a = b\}$$

else

$$a + 1 = b \wedge b \leq c$$

$$a = a + 1$$

$$Q \equiv \{a = b\}$$

$$\frac{\begin{array}{l} \{P \wedge B\} S_1 \{Q\} \\ \{P \wedge \neg B\} S_2 \{Q\} \end{array}}{\{P\} \text{ if } B \text{ then } S_1 \text{ else } S_2 \{Q\}}$$

$$P \equiv \{?\}$$

while (a>b)

$$P \wedge a > b$$

$$b = b - a$$

$$c = c / 2$$

$$P \equiv \{?\}$$

$$P \wedge a \leq b \equiv c = b - a$$

$$\frac{\{P \wedge B\} S \{P\}}{\{P\} \text{ while } B \text{ do } S \{P \wedge \neg B\}}$$

$$P \equiv \{?\}$$

while (a>b)

$$P \wedge a > b$$

$$b = b - a$$

$$c / 2 = b - a$$

$$c = c / 2$$

$$P \equiv \{?\}$$

$$P \wedge a \leq b \equiv c = b - a$$

$$\frac{\{P \wedge B\} S \{P\}}{\{P\} \text{ while } B \text{ do } S \{P \wedge \neg B\}}$$

$$P \equiv \{?\}$$

while (a>b)

$$c/4 = b - 3a$$

$$b = b - a$$

$$c/4 = b - 2a$$

$$c = c/2$$

$$c/2 = b - 2a$$

$$\frac{\{P \wedge B\} S \{P\}}{\{P\} \text{ while } B \text{ do } S \{P \wedge \neg B\}}$$

$$P \equiv \{?\}$$

while (a>b)

$$c/4 = b - 3a$$

$$b = b - a$$

$$c/4 = b - 2a$$

$$c = c/2$$

$$c/2 = b - 2a$$

$$\frac{\{P \wedge B\} S \{P\}}{\{P\} \text{ while } B \text{ do } S \{P \wedge \neg B\}}$$

$$c/2^i = b - (i+1)a$$

$$c / 2^i = b - (i + 1)a, i \in \mathbb{N}, a > b$$

$$\{P \wedge B\} S \{P\}$$

while (a>b)

$$\frac{\{P \wedge B\} S \{P\}}{\{P\} \text{ while } B \text{ do } S \{P \wedge \neg B\}}$$

$$c / 2^i = b - (i + 1)a \wedge a > b$$

$$b = b - a$$

$$c / 2^i = b - ia$$

$$c = c / 2$$

$$c / 2^{l-1} = b - ia$$

$$c = b - a \wedge a \leq b$$

$$c / 2^i = b - (i + 1)a, i \in \mathbb{N}, a > b$$

while (a>b)

$$c / 2^i = b - (i + 1)a \wedge a > b$$

$$b = b - a$$

$$c / 2^i = b - ia$$

$$c = c / 2$$

$$c / 2^{l-1} = b - ia$$

$$\frac{\{P \wedge B\} S \{P\}}{\{P\} \text{ while } B \text{ do } S \{P \wedge \neg B\}}$$